

III B. TECH I SEMESTER REGULAR EXAMINATIONS, FEB - 2022
FINITE ELEMENT METHODS
(MECHANICAL ENGINEERING)

Time: 3 Hours

Max. Marks: 60

Note: Answer **ONE** question from each unit ($5 \times 12 = 60$ Marks)

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UNIT-I

1. a) Differentiate plane stress and plane strain problems with suitable examples. [6M]
- b) Determine the strain components  $\epsilon_x$ ,  $\epsilon_y$  and  $\gamma_{xy}$  for the displacement field [6M]

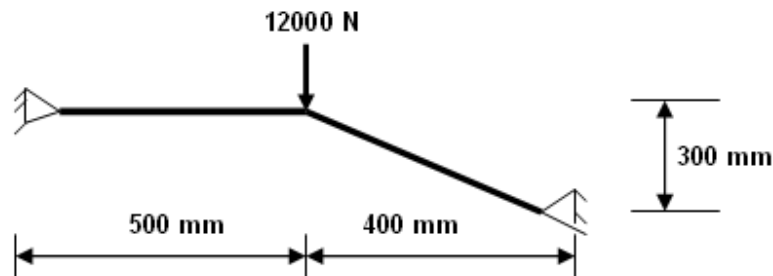
$$u = 2x^2 + 2y^2 + 6xy \quad \text{and} \quad v = 3x + 6y - 2y^2 \quad \text{at the point } x = -1, y = 0.$$

(OR)

2. a) Describe the basic steps involved in finite element analysis. [6M]
- b) Discuss the various element shapes in FEA. [6M]

UNIT-II

3. Compute the displacements at nodes in elements shown in figure. [12M]  
 Take the Modulus of Elasticity as  $70,000 \text{ N/mm}^2$  and  $A=200 \text{ mm}^2$ .



(OR)

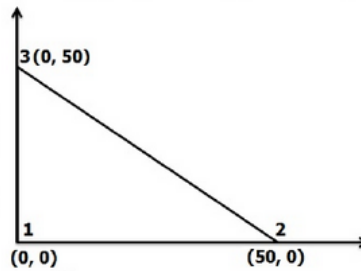
4. Show that the central deflection of the beam of length  $L$  m (both the ends are fixed) carries a load of  $W$  at the center is given by  $WL^3/192 EI$  using FEM by dividing the beam into two elements. [12M]

UNIT-III

5. a) Discuss the properties of constant-strain triangular element. [6M]
- b) The nodal coordinates of a triangular element are 1(1,3), 2(5,3) and 3(4,6). [6M]  
 At a point 'P' inside the element, the x-coordinates is 3.3 and the shape function  $N_1 = 0.3$ . Determine the shape functions and y-coordinates of the point P.

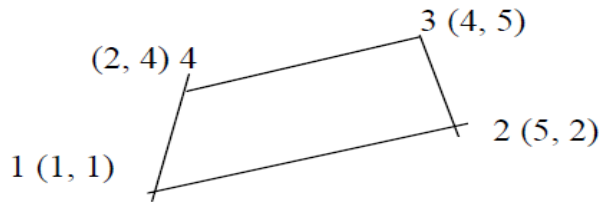
(OR)

6. Evaluate the stiffness matrix for the axi-symmetric element shown in Figure. [12M]  
Take the Modulus of Elasticity as  $2.1 \times 10^5 \text{ N/mm}^2$  and Poisson's ratio as 0.3.



UNIT-IV

7. Find the Jacobian determinant [J] of the two dimensional element at  $\xi=0$  and  $\eta=0$  as shown in figure. [12M]



(OR)

8. a) Describe about Gauss quadrature technique in numerical integration. [6M]  
b) Check what order of the Gauss quadrature could exactly integrate the following. [6M]

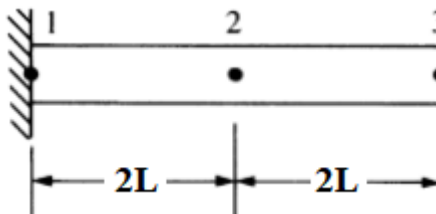
$$\Phi = (2 + 3x + 5x^3 + 8x^6).$$

UNIT-V

9. A metallic fin with thermal conductivity  $k=360 \text{ W/m}^\circ\text{C}$ , 0.001 m thick and 0.1m long, extends from a plane wall whose temperature is  $235^\circ\text{C}$ . Determine the temperature distribution and amount of heat transferred from the fin to the air at  $20^\circ\text{C}$  with  $h=9 \text{ W/m}^2\text{C}$ . Take the width of fin to be 1 m. [12M]

(OR)

10. Determine the Eigen values and Eigen vectors of the bar shown in figure. Take [12M]  
 $E = 200 \text{ Gpa}$ ,  $\rho = 7862 \text{ kg/m}^2$ ,  $A = 6 \text{ cm}^2$  and  $L = 2.5 \text{ m}$ .



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